## Exercise 1 - Crystal Structure

(a) The primitive vectors for a *body center cubic* (bcc) lattice are

$$egin{array}{rcl} ec{a}_1 &=& aec{x}, \ ec{a}_2 &=& aec{y}, \ ec{a}_3 &=& \dfrac{a}{2}(ec{x}+ec{y}+ec{z}). \end{array}$$

or, in a more symmetric set

$$\vec{a}_1 = \frac{a}{2}(-\vec{x} + \vec{y} + \vec{z}),$$
  

$$\vec{a}_2 = \frac{a}{2}(\vec{x} - \vec{y} + \vec{z}),$$
  

$$\vec{a}_3 = \frac{a}{2}(\vec{x} + \vec{y} - \vec{z}).$$

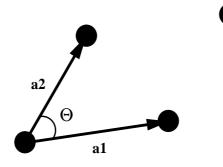
- 1. Make a drawing of this lattice,
- 2. Find the reciprocal lattice vectors and make a drawing of the reciprocal lattice.
- (b) The primitive vectors for a *face center cubic* (fcc) lattice are

$$\vec{a}_1 = \frac{a}{2}(\vec{y} + \vec{z}),$$

$$\vec{a}_2 = \frac{a}{2}(\vec{x} + \vec{z}),$$

$$\vec{a}_3 = \frac{a}{2}(\vec{x} + \vec{y}).$$

- 1. Make a drawing of this lattice,
- 2. Find the reciprocal lattice vectors and make a drawing of the reciprocal lattice.
- (c) Graphically construct the Wigner-Seitz cell and the reciprocal lattice of the two dimensional oblique lattice with basis vectors  $\vec{a}1$  and  $\vec{a}2$  shown in the following sketch:



(3 points)

SS 2011 Sheet 1

(1 points)

## Exercise 2 - The Brillouin Zone

Show that the volume of the elementary cell  $\Omega$  and the volume of the Brillouin Zone  $\Omega_B$  are connected by the following relation:

$$\Omega_B = \frac{(2\pi)^3}{\Omega} \tag{1}$$

## Exercise 3 - Tetragonal symmetry (2 points)

Show that if one streches a fcc lattice along one of its lattice vectors, the resulting lattice is equivalent to a tetragonal body centered lattice. So the point group with the tetragonal symmetry has two Bravais lattices: simple tetragonal and body centered tetragonal, whereas the point group with cubic symmetry has three Bravais lattices: sc, bcc and fcc.

## Exercise 4 - Fourier transformations

- 1. Calculate the Fourier coefficients for a function f(x) = c, c some number, x defined in some one-dimensional interval.
- 2. Calculate explicitly the Fourier coefficients for a function  $f(x) = \exp(ip\frac{2\pi}{a}x)$ , with p some integer.

Solutions due on: 6 May, 2011

(2 points)